

Cambridge O Level

CANDIDATE NAME		
CENTRE NUMBER		CANDIDATE NUMBER
ADDITIONAL	MATHEMATICS	4037/13
Paper 1		October/November 2021
		2 hours

You must answer on the question paper.

No additional materials are needed.

INSTRUCTIONS

- Answer **all** questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

INFORMATION

- The total mark for this paper is 80.
- The number of marks for each question or part question is shown in brackets [].

This document has 16 pages. Any blank pages are indicated.

Mathematical Formulae

1. ALGEBRA

Quadratic Equation

For the equation $ax^2 + bx + c = 0$,

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Binomial Theorem

$$(a+b)^{n} = a^{n} + \binom{n}{1}a^{n-1}b + \binom{n}{2}a^{n-2}b^{2} + \dots + \binom{n}{r}a^{n-r}b^{r} + \dots + b^{n}$$

where *n* is a positive integer and $\binom{n}{r} = \frac{n!}{(n-r)!r!}$

Arithmetic series
$$u_n = a + (n-1)d$$

 $S_n = \frac{1}{2}n(a+l) = \frac{1}{2}n\{2a + (n-1)d\}$
Geometric series $u_n = ar^{n-1}$

$$S_n = \frac{a(1-r^n)}{1-r} \ (r \neq 1)$$
$$S_{\infty} = \frac{a}{1-r} \ (|r| < 1)$$

2. TRIGONOMETRY

Identities

$\sin^2 A + \cos^2 A = 1$
$\sec^2 A = 1 + \tan^2 A$
$\csc^2 A = 1 + \cot^2 A$

Formulae for $\triangle ABC$

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$
$$a^{2} = b^{2} + c^{2} - 2bc \cos A$$
$$\Delta = \frac{1}{2}bc \sin A$$

1 On the axes below, sketch the graph of $y = -\frac{1}{4}(2x+1)(x-3)(x+4)$ stating the intercepts with the coordinate axes. [3]



2 A particle moves in a straight line such that its velocity, $v \text{ ms}^{-1}$, at time *t* seconds after passing through a fixed point *O*, is given by $v = e^{3t} - 25$. Find the speed of the particle when t = 1. [2]

3 Solve the equation $\cot^2\left(2x - \frac{\pi}{3}\right) = \frac{1}{3}$, where *x* is in radians and $0 \le x < \pi$. [5]

4

4 (a) Find the first three terms, in ascending powers of x^2 , in the expansion of $\left(\frac{1}{2} - \frac{2}{3}x^2\right)^8$. Write your coefficients as rational numbers. [3]

(**b**) Find the coefficient of x^2 in the expansion of $\left(\frac{1}{2} - \frac{2}{3}x^2\right)^8 \left(2x + \frac{1}{x}\right)^2$. [3]

- 5 A geometric progression is such that its sum to 4 terms is 17 times its sum to 2 terms. It is given that the common ratio of this geometric progression is positive and not equal to 1.
 - (a) Find the common ratio of this geometric progression. [3]

(b) Given that the 6th term of the geometric progression is 64, find the first term. [2]

(c) Explain why this geometric progression does not have a sum to infinity. [1]

https://xtremepape.rs/

6 (a) A 5-digit number is made using the digits 0, 1, 2, 3, 4, 5, 6, 7, 8 and 9. No digit may be used more than once in any 5-digit number. Find how many such 5-digit numbers are odd and greater than 70 000. [3]

(b) The number of combinations of *n* objects taken 3 at a time is 2 times the number of combinations of *n* objects taken 2 at a time. Find the value of *n*. [4]

8



The diagram shows a circle, centre O, radius 10 cm. The points A, B and P lie on the circumference of the circle. The chord AB is of length 14 cm. The point Q lies on AB and the line POQ is perpendicular to AB.

(a) Show that angle *POA* is 2.366 radians, correct to 3 decimal places.

(b) Find the area of the shaded region.

[3]

[2]

(c) Find the perimeter of the shaded region.

[5]

- 8 The curves $y = x^2 + x 1$ and $2y = x^2 + 6x 2$ intersect at the points *A* and *B*.
 - (a) Show that the mid-point of the line *AB* is (2, 9).

The line l is the perpendicular bisector of AB.

(b) Show that the point C(12, 7) lies on the line *l*.

[3]

[5]

(c) The point D also lies on l, such that the distance of D from AB is two times the distance of C from AB. Find the coordinates of the two possible positions of D. [4]

https://xtremepape.rs/

- 9 When e^{2y} is plotted against x^2 , a straight line graph passing through the points (4, 7.96) and (2, 3.76) is obtained.
 - (a) Find y in terms of x.

[5]

(b) Find y when x = 1.

[2]

(c) Using your equation from part (a), find the positive values of x for which the straight line exists. [3]

- **10** A curve with equation y = f(x) is such that $\frac{d^2 y}{dx^2} = (2x+3)^{-\frac{1}{2}} + 5$ for x > 0. The curve has gradient 10 at the point $(3, \frac{19}{2})$.
 - (a) Show that, when x = 11, $\frac{dy}{dx} = 52$. [5]

(b) Find f(x).

[4]

11 A curve has equation $y = \frac{(x^2 - 5)^{\frac{1}{3}}}{x+1}$ for x > -1.

(a) Show that
$$\frac{dy}{dx} = \frac{Ax^2 + Bx + C}{3(x+1)^2 (x^2 - 5)^{\frac{2}{3}}}$$
 where *A*, *B* and *C* are integers. [6]

(b) Find the *x*-coordinate of the stationary point on the curve.

(c) Explain how you could determine the nature of this stationary point. [You are not required to find the nature of this stationary point.] [2]

[2]

BLANK PAGE

Permission to reproduce items where third-party owned material protected by copyright is included has been sought and cleared where possible. Every reasonable effort has been made by the publisher (UCLES) to trace copyright holders, but if any items requiring clearance have unwittingly been included, the publisher will be pleased to make amends at the earliest possible opportunity.

To avoid the issue of disclosure of answer-related information to candidates, all copyright acknowledgements are reproduced online in the Cambridge Assessment International Education Copyright Acknowledgements Booklet. This is produced for each series of examinations and is freely available to download at www.cambridgeinternational.org after the live examination series.

Cambridge Assessment International Education is part of the Cambridge Assessment Group. Cambridge Assessment is the brand name of the University of Cambridge Local Examinations Syndicate (UCLES), which itself is a department of the University of Cambridge.

© UCLES 2021